# OPEN STUDENT FOUNDATION 

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## * Answer The Following Questions as Directed.

1. If $\bar{x}=30, \bar{y}=20$ and $b=0.6$, find the intercept of the regression line of $Y$ on $X$ and write equation of the line.
2. If $b=1.5, r=0.8$ and standard deviation of $X$ is 1.6 , find the standard deviation of $Y$.
3. The fitted regression line of $Y$ on $X$ is $\hat{\mathbf{y}}=23.2-1.2 x$ and one of the observations used in fitting of the line is $(6,17)$. Find the error in estimating $Y$ for $X=6$.
4. If the regression coefficient of the regression line of $Y$ on $X$ in 0.6 and the standard deviations of $X$ and $Y$ are 5 and 3 respectively, find the coefficient of determination.
5. If the regression line of $Y$ on $X$ is $\hat{y}=35+2 x$ and $\operatorname{Cov}(x, y)=50$, find the standard deviation of $X$.
6. For the regression line given in the previous question (7)m if the value of $Y$ is to be increased by 10 units, how many units should be increased in the value of $X$ ?
7. If $b_{y x}=0.75, u=6(x-20)$ and $v=2(y-15)$ for the data in the study of a regression line then find the value of $b_{v u}$.
8. If the regression line of $Y$ on $X$ is $\hat{y}=12-1.5 x$ and the mean of $X$ is 6 , find the mean of $Y$.
9. If the regression line of $Y$ on $X$ is $\hat{y}=11.5+0.65 x$ and $\bar{y}=18$, find $\bar{x}$.
10. The fitted regression line of $Y$ on $X$ is $\hat{y}=50+3.5 x$. If an observation $(16,108)$ is used in fitting of the line, find the error in estimating $Y$ for $X=16$.
11. If one observation $(10,30)$ is used in the fitting of the line $\hat{y}=22+0.8 x$, find the error in estimating $Y$ for $X=10$. What can you deduce from the value of the error ?
12. If $b_{y x}=0.85, u=x-15$ and $v=y-20$, find the value of $b_{v u}$.
13. If $u=\frac{x-5}{3}, v=\frac{y-8}{5}$ and $b_{y x}=0.9$, find the value of $b_{v u}$.
14. If $u=10(x-4.5), v=\frac{y-50}{10}$ and $b_{y x}=0.25$, find the value of $b_{v u}$.
15. If $u=5(x-40), v=2(y-18)$ and $b_{y x}=1.6$, find the value of $b_{v u}$.

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16. State the utility of regression.
17. If $b_{y x}=0.8$ then find the value of $b_{v u}=$ for the following $u$ and $v$.
(i) $u=x-105$ and $v=y-90$
(ii) $u=\frac{x-1400}{100}$ and $v=\frac{y-750}{50}$
(iii) $u=10(x-4.6)$ and $v=y-75$
18. If $\bar{x}=30, \bar{y}=50, r=0.8$ and the standard deviations of $X$ and $Y$ are 2 and 5 respectively obtain the regression line of $Y$ on $X$.
19. If the regression line of $Y$ on $X$ is $\hat{y}=11+3 x$ and $S_{x}: S_{y}=3: 10$, find the co-efficient of determination.
20. If $\bar{x}=5, \bar{y}=11$ and $b=1.2$, obtain the regression line of $Y$ on $X$.
21. If $\bar{x}=60, \bar{y}=75$ and $s_{x}^{2}: \operatorname{Cov}(x, y)=5: 3$, obtain the regression line of $Y$ on $X$ and estimate $y$ for $X=65$ from it.

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22. The information of price (in ₹) of a ballpen and the supply of ballpen (in units) at the end of each month of a year for a company making ball pen is given below. Estimate the supply of ballpen when its price is ₹ 40 .

| Detail | Price (x) | Supply (y) |
| :--- | :---: | :---: |
| Average | 30 | 500 |
| Variance | 25 | 10,000 |
| $r=0.8$ |  |  |

23. The electricity is generated by windmill manufactured by a company. The following information is obtained by recording five observations regarding the velocity of wind (km per hour) and generation of electricity (in Watts) by a unit of the company.
Velocity of Wind $=X \mathrm{~km}$ per hour
Electricity Generation $=\mathrm{Y}$ Watts
$\bar{x}=20, \bar{y}=186, \Sigma x y=23200, s_{x}^{2}=50$
Obtain the regression line of electricity generation $(\mathrm{Y})$ on velocity of wind $(\mathrm{X})$. Estimate the electricity generation if the velocity of wind is 25 km per hour.
24. Six pairs of father-son are selected in a sample of an experiment to know the relation between the heights of fathers in $\mathrm{cm}(\mathrm{X})$ and the heights of their adult sons in em ( Y ). The following results are obtained from it.
$\Sigma x=1020, \Sigma y=990, \Sigma(x-170)^{2}=60, \Sigma(y-165)^{2}=105$
$\Sigma(x-170)(y-165)=45$
Obtain the regression line of the heights of sons $(\mathrm{Y})$ on the heights of fathers $(\mathrm{X})$. Also verify the reliability of the regression model.
25. (i) If the regression line is $\hat{y}=\frac{x}{2}+5$ and $s_{y}: s_{x}=5: 8$, find the coefficient of determination.
(ii) If the regression line of $Y$ on $X$ is $4 x+5 y-65=0$, find the value of regression coefficient $b$.
26. The following information is obtained to study the relationship between average rainfall (in cm ) and the yield of maize (in quintal per hectare) in different talukaa of Gujarat:

| Particulars | Rainfall (cm) <br> $\boldsymbol{x}$ | Yield of Maize (Quintal per Hectare) <br> $\boldsymbol{y}$ |
| :--- | :---: | :---: |
| Mean | 82 | 180 |
| Variance | 64 | 225 |
| Correlation coefficient $=0.82$ |  |  |

Estimate the yield of maize when the rainfall is 60 cm .
27. The following results are obtained to study the relation between the price of battery (cell) of wrist watch in rupees (X) and its supply in hundred units $(Y)$ :
$n=10, \Sigma x=130, \Sigma y=220, \Sigma x^{2}=2288$ and $\Sigma x y=3467$
Obtain the regression line of $Y$ on $X$ and estimate the supply when price is $₹ 16$.
28. The information regarding maximum temperature $(\mathrm{X})$ and sale of ice cream ( Y ) of six different days in summer for a city is given below : Maximum temperature $=\mathrm{X}$ (in celsius). Sale of ice cream $=Y$ (in lakh ₹) $\bar{x}=40, \bar{y}=1.2, \Sigma x y=306, S \times 2=20$ Obtain the regression line of sale of ice cream on maximum temperature. Estimate the sale of ice cream if the maximum temperature on a day is 42 Celsius.

* Calculate The Following Sums In Detail.

29. The information regarding the experience (In years) of eight workers on a machine and their performance ratings based on the non-defective units they manufactured in every 100 units is as follows :

| Experience of worker (years) | 5 | 12 | 15 | 8 | 20 | 18 | 22 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Performance rating | 80 | 82 | 85 | 81 | 90 | 90 | 95 | 97 |

Obtain the regression line of the performance rating on the experience and estimate the performance rating if a worker has an experience of 17 years.
30. Obtain the regression line of $Y$ on $X$ from the following data and estimate $Y$ for $X=30$.
$n=10, x=250, y=300, x y=7900, x^{2}=6500$.
31. The following results are obtained from the information of average rain and yield of a crop per acre in the last ten years of an arid region :

| Particulars | Rainfall <br> $(\mathbf{c m})$ | Yield of crop <br> $(\mathbf{k g})$ |
| :--- | :---: | :---: |
| Mean | 18 | 970 |
| Standard Deviation | 2 | 38 |
| Correlation Coefficient $=0.6$ |  |  |

Estimate the yield of the crop if it rains 20 cms .
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